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ESE-2025 : Main Examination Civil Engineering : Paper-II

Civil Engineering : Paper-II | Conventional Solved Questions : (2000-2024)

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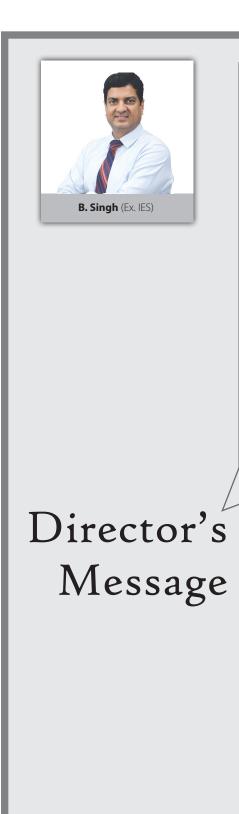
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During the last few decades of engineering academics, India has witnessed geometric growth in engineering graduates. It is noticeable that the level of engineering knowledge has degraded gradually, while on the other hand competition has increased in each competitive examination including GATE and UPSC examinations. Under such scenario higher level efforts are required to take an edge over other competitors.

The objective of **MADE EASY books** is to introduce a simplified approach to the overall concepts of related stream in a single book with specific presentation. The topic-wise presentation will help the readers to study & practice the concepts and questions simultaneously.

The efforts have been made to provide close and illustrative solutions in lucid style to facilitate understanding and quick tricks are introduced to save time.

Following tips during the study may increase efficiency and may help in order to achieve success.

- Thorough coverage of syllabus of all subjects
- Adopting right source of knowledge, i.e. standard reading text materials
- Develop speed and accuracy in solving questions
- Balanced preparation of Paper-I and Paper-II subjects with focus on key subjects
- Practice online and offline modes of tests
- Appear on self assessment tests
- Good examination management
- Maintain self motivation
- Avoid jumbo and vague approach, which is time consuming in solving the questions
- Good planning and time management of daily routine
- Group study and discussions on a regular basis
- Extra emphasis on solving the questions
- Self introspection to find your weaknesses and strengths
- Analyze the exam pattern to understand the level of questions
- Apply shortcuts and learn standard results and formulae to save time

B. Singh (Ex. IES) CMD, MADE EASY Group

Civil Engineering

Conventional Solved Questions

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Paper-II

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Fluid Mechanics, Hydraulic **Machines and OCF**

Revised Syllabus of ESE : Fluid Mechanics, Open Channel Flow, Pipe Flow: Fluid properties; Dimensional Analysis and Modeling; Fluid dynamics including flow kinematics and measurements; Flow net; Viscosity, Boundary layer and control, Drag, Lift, Principles in open channel flow, Flow controls. Hydraulic jump; Surges; Pipe networks.

Hydraulic Machines and Hydro power: Various pumps, Air vessels, Hydraulic turbines – types, classifications & performance parameters; Power house – classification and layout, storage, pondage, control of supply.

1. Fluid Properties

A plate with surface area of 0.4 m² and weight of 500 N slides down on an inclined plane at 30° to 1.1 the horizontal at a constant speed of 4 m/s. If the inclined plane is lubricated with an oil of dynamic viscosity 2 poise, find the thickness of lubricant film.

[10 marks : 2006]

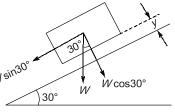
Solution:

...

Assuming linear relations the lubricant and velocity	in	
Let the thickness of the lu	30°	
Surface Area of plate,	$A = 0.4 \text{ m}^2$	Wsin30°
Weight of plate,	$W = 500 \mathrm{N}$	30° W W

Speed of sliding of plate, V = 4 m/s

Dynamic viscosity, $\mu = 2$ poise = 0.2 kg/m-s



The shear stress will be developed in the lubricant due to the component of the weight of the plate in the direction of motion. Let the component of weight in the direction of motion be F.

$$F = Wsin30^{\circ} = 500 sin 30^{\circ} = 250 N$$

According to Newton's law of viscosity,

$$F = \frac{\mu AV}{y}$$

$$\Rightarrow \qquad 250 = \frac{0.2 \times 0.4 \times 4}{y}$$

$$\Rightarrow \qquad y = 1.28 \times 10^{-3} \text{ m}$$

$$= 1.28 \text{ mm}$$

$$\therefore F = \tau A; \qquad \tau = \mu \frac{du}{dy}$$

1.2 A rotating viscometer has two cylinders. The radius of inner fixed cylinder is R_1 and the radius of the outer rotating cylinder is R_2 . This viscometer is used for the measurement of viscosity. Derive an expression for the viscosity in terms of the torque acting on the inner cylinder of height L, gap between the bottoms of the two cylinders *b*, and the angular speed ω (omega).

[9 marks : 2007]

Solution:

It consists of two co-axial cylinders, having radius R_1 and R_2 as shown in the figure. The very small space $(R_2 - R_1)$ is left in between the two. The space between them is filled with the liquid whose viscosity is to be determined.

The inner cylinder is suspended by a torsion wire on spring and it is held stationary. The outer cylinder is then rotated at a constant angular velocity. When the outer cylidner rotates, the torque generated by such rotation is transmitted by the thin liquid film to the inner stationary cylinder, which causes rotation of torsion wire. The rotation of wire can be measured by means of a circular dial attached to the wire and a fixed pointer.

From the previously obtained calibration curve between the torque and the rotation of torsion wire, the torque exerted on wire and hence on the inner cylinder, corresponding to the measured rotation of wire can be known.

Total torque,

$$T = T_1 + T_2$$

$$T_1 = \text{Torque due to side}$$

$$T_2 = \text{Torque due to bottom}$$

Case-1:

Torque contributed from the sides, T_1

Circumferential velocity of the outer cylinder

 $V = \omega R_2$ Clearance between the cylinders, $h = R_2 - R_1$ Assuming linear variation of velocity across the gap,

Velocity gradient
$$\frac{du}{dr} = \frac{V}{r} = \frac{\omega R_2}{R_2 - R_1}$$

Shear stress,

 \Rightarrow

$$= \mu \frac{du}{dr} = \frac{\mu \omega R_2}{R_2 - R_2}$$

 $F_s = \tau \times 2\pi R_1 \times L$

Shear force,

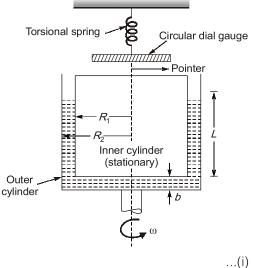
$$\therefore \qquad \qquad T_1 = F_s \times R_1$$

 \Rightarrow

$$T_{1}^{'} = \tau \times 2\pi R_{1} \times L \times R_{1}$$
$$T_{1} = \frac{\mu \omega R_{2}}{(R_{2} - R_{1})} \times 2\pi R_{1}^{2} L$$

τ

$$= \frac{2\pi\mu\omega R_1^2 R_2 L}{R_2 - R_1}$$
...(ii)



Case-2:

Torque contributed from the bottom (T_2)

Consider an element of inner cylinder of width 'dr' at a radial distance r.

 $V = I \omega$

Velocity at this radius,

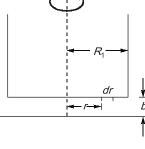
Assuming linear variation of velocity with depth in the gap 'b'

Shear stress,

$$\tau = \frac{\mu v}{b} = \frac{\mu r \omega}{b}$$

Torque of the element,

$$dT_2 = \frac{\mu r \omega}{b} (2\pi r \, dr) r = \frac{\mu \omega}{b} 2\pi r^3 dr$$



Total torque on the cylinder, $T_2 = \int_0^{R_1} \frac{\mu \omega}{b} 2\pi r^3 dr$

 $T_2 = \frac{\mu\omega}{b} 2\pi \left[\frac{r^4}{4}\right]_0^{R_1} = \frac{\mu\omega}{b} \frac{2\pi R_1^4}{4} = \frac{\pi\mu\omega R_1^4}{2b}$

Total torque,

 \Rightarrow

$$T = \frac{2\pi\mu\omega R_1^2 R_2 L}{R_2 - R_1} + \frac{\pi\mu\omega}{2k}$$

 $T = T_1 + T_2$

$$T = \left(\frac{2\pi R_1^2 R_2 L}{R_2 - R_1} + \frac{\pi R_1^4}{2b}\right) \omega \mu$$
$$\mu = \frac{T}{\omega \left(\frac{2\pi R_1^2 R_2 L}{R_2 - R_1} + \frac{\pi R_1^4}{2b}\right)}$$

• •

- **1.3** Through a very narrow gap of height '*h*' a thin plate of large extent is pulled at a velocity *V*. On one side of the plate oil of viscosity μ_1 and on other side oil of viscosity μ_2 . Calculate the position of plate so that:
 - (i) The shear force on two sides of plate is equal
 - (ii) The pull required to drag the plate is minimum

Solution:

Let *y* be the distance of the thin plate from the top surface. Assuming linear relationship between shear stress developed and the velocity gradient.

(i) Shear stress developed on the top portion is given by,

$$\tau_1 = \mu_1 \frac{du}{dy}$$
$$\tau_1 = \mu_1 \times \frac{V}{V}$$

 \Rightarrow

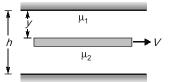
Shear stress developed on the bottom portion is given by

$$\tau_2 = \mu_2 \times \frac{V}{h-y}$$

If A is the area of thin plate, then shear force on the top and bottom portion,

$$F_1 = \tau_1 \times A$$
 and $F_2 = \tau_2 \times A$

[10 marks: 2008]



... (iii)

 $F_1 = F_2$ $\tau_1 \times A = \tau_2 \times A$ But \Rightarrow $\mu_1 \times \frac{V}{v} = \mu_2 \times \frac{V}{h-v}$ \Rightarrow $\mu_1(h-y) = \mu_2 y$ \Rightarrow $y(\mu_1 + \mu_2) = \mu_1 h$ \Rightarrow $y = \frac{\mu_1 h}{\mu_1 + \mu_2}$ (Ans.) \Rightarrow (ii) The pull required to drag the plate = Total shear force $F = F_1 + F_2$ \Rightarrow $F = \tau_1 A + \tau_2 A$ \Rightarrow $F = \mu_1 \times \frac{V}{V} \times A + \mu_2 \times \frac{V}{h - V} \times A = \left[\frac{\mu_1}{V} + \frac{\mu_2}{h - V}\right] VA$ \Rightarrow $\frac{dF}{dV} = 0$ For F to be minimum, $-\frac{\mu_1}{v^2} + \frac{\mu_2}{(h-v)^2} = 0$ \Rightarrow $\frac{y^2}{(h-y)^2} = \frac{\mu_1}{\mu_2}$ \Rightarrow $\frac{y}{h-y} = \frac{\sqrt{\mu_1}}{\sqrt{\mu_2}}$ \Rightarrow $\left(\sqrt{\mu_1} + \sqrt{\mu_2}\right)y = \sqrt{\mu_1}h$ \Rightarrow $y = \frac{\sqrt{\mu_1} h}{\sqrt{\mu_1} + \sqrt{\mu_2}}$ (Ans.) \Rightarrow

1.4 The velocity distribution for flow over a plate is given by

$$u=2y-y^2$$

in which u is the velocity in ms⁻¹ at a distance y metres from the plate. Determine the shear stress in Nm⁻² at the boundary and at 0.2 m from it. Dynamic viscosity of fluid is 0.9 Ns/m².

[4 marks : 2013]

Solution:

Given $u = 2y - y^2$ and $\mu =$ Dynamic viscosity of fluid = 0.9 Ns/m²

Shear stress
$$(\tau) = \mu \frac{\partial u}{\partial y} = \mu (2 - 2y)$$

$$\therefore \qquad \tau|_{y=0.2\,\text{m}} = 0.9(2-2\times0.2) = 1.44\,\text{N/m}^2$$

and
$$\tau_{1_{Y=0}} = 0.9\times2 = 1.8\,\text{N/mm}^2$$

1.5 A rectangular plate of $0.50 \text{ m} \times 0.50 \text{ m}$ dimensions weighing 500 N slides down an inclined plane making 30° angle with the horizontal, at a velocity of 1.75 m/s. If the 2 mm gap between the plate and the inclined surface is filled with a lubricating oil, find its viscosity and express it in poise as well as in Ns/m².

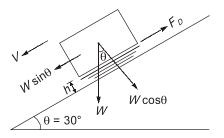
Solution:

A=0.25 m $A = 0.50 \times 0.50 = 0.25 \,\mathrm{m}^2$ Area of plate, $W = 500 \, \text{N}$ Weight of plate, 2000 V=1.75mls $W\sin\theta = F_{drag}$ 500 sin 30° = $\tau \cdot A$ Wsinθ $\mu \frac{du}{dv} A = 500 \sin 30^{\circ}$ W/ Wcosθ \Rightarrow 30° $\mu \frac{(V-0)}{2 \times 10^{-3}} \times 0.25 = 500 \sin 30^{\circ}$ \sim \rightarrow $\mu = \frac{500 \sin 30^{\circ} \times 2 \times 10^{-3}}{1.75 \times 0.25} = 1.143 \text{ N-s/m}^2$ $1 \text{ Poise} = 10^{-1} \text{ N-s/m}^2$ Since; $1\frac{N-s}{m^2} = 10$ Poise \Rightarrow $\mu = 11.43$ poise or 1.143 N-s/m² *.*..

1.6 A rectangular plate of 0.5 m × 0.5 m dimensions, weighing 500 N slides down an inclined plane making 30° angle with the horizontal at a velocity of 1.75 m/s. If the 2 mm gap between the plate and inclined surface is filled with a lubricating oil, find its viscosity in poise.

[6 marks : 2020]

Solution:



Force analysis in direction of motion

$$F_{D} = W \sin \theta$$

$$\tau A = 500 \sin 30^{\circ} \qquad ...(i)$$

$$\tau = \mu \frac{du}{dy}$$

∴ Shear stress,

{Since the gap is very-very small so velocity variation is considered as linear.}

$$\tau = \mu \frac{V - 0}{h}$$
$$\tau = \mu \frac{V}{h}$$

[4 marks : 2014]

$$\mu \frac{V}{h}A = 500 \sin 30^{\circ}$$
$$\mu \frac{(1.75)}{0.002} \times 0.5 \times 0.5 = 500 \sin 30^{\circ}$$
$$\mu = 1.143 \text{ Ns/m}^2$$
$$\mu = 11.43 \text{ Poise}$$

1.7 A rectangular plate of 0.50 m \times 0.50 m dimensions and weighing 500 N slides down an inclined plane making 30° angle with the horizontal. The velocity of the plate is 1.75 m/s. If the 2 mm gap between the plate and the inclined surface is filled with lubricating oil, find the viscosity of oil and express it in units of poise as well as N-s/m². Assume the plate as frictionless.

[12 marks : 2024]

Solution:

Given: Angle of inclination, $\theta = 30^{\circ}$ Area of plate, $A = 0.5 \text{ m} \times 0.5 \text{ m} = 0.25 \text{ m}^2$ Weight of plate, W = 500 NVelocity of plate, V = 1.75 m/sGap between plate and surface, $h = 2 \text{ mm} = 2 \times 10^{-3} \text{ m}$

On the plate, drag force will act due to shear resistance between plate and oil.

Now, Drag force, $F_D = W \sin 30^\circ$ $\Rightarrow \qquad \tau A = 500 \sin 30^\circ$

where $\boldsymbol{\tau}$ is shear stress acting on plate

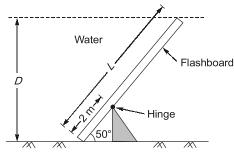
$$\Rightarrow \qquad \mu\left(\frac{V-0}{h}\right) \times A = 250$$

where $\boldsymbol{\mu}$ is coefficient of viscosity

$$\Rightarrow \quad \mu\left(\frac{1.75}{2 \times 10^{-3}}\right) \times 0.5 \times 0.5 = 250$$
$$\Rightarrow \qquad \mu = 1.143 \text{ N-s/m}^2 = 11.43 \text{ poise}$$

2. Manometry and Hydrostatic Forces

2.1 Find the depth of water required to topple the rectangular flashboard and reaction at the hinge of the flashboard shown in figure.



Solution:

Let the centre of gravity of the flashboard be at a distance \overline{x} from the free surface.

 $500 \sin 30^{\circ}$ 30° 30° $500 \cos 30^{\circ}$ 500

[10 marks : 2006]

Assuming unit width of the flashboard perpendicular to the plane of paper

Hydrostatic force on the flashboard is given by

$$F = wA\overline{x} = w(L \times 1) \times \overline{x} = wL\overline{x}$$

$$\sin 50^{\circ} = \frac{D}{L} = \frac{\overline{x}}{L/2}$$

$$\overline{x} = \frac{L}{2} \sin 50^{\circ} \text{ and } D = L \sin 50^{\circ}$$

...

...

$$F = wL\overline{x}$$
 [:: Area = $L \times 1$, for unit width]

$$\Rightarrow \qquad F = wL \times \frac{L}{2} \sin 50^\circ = \frac{wL^2}{2} \sin 50^\circ$$

The hydrostatic force *F* will act at the centre of pressure (\overline{h}) .

$$\therefore \qquad \overline{h}_{cp} = \overline{x} + \frac{I_G}{A\overline{x}} \sin^2 \theta$$

$$\overline{h}_{cp} = \frac{L}{2}\sin 50^\circ + \frac{1 \times L^3 \times 2}{12 \times (L \times 1) \times L \sin 50^\circ} \sin^2 50^\circ \qquad \left[\because I_G = \frac{bd^3}{12} = \frac{1 \times L^3}{12} \right]$$
$$= \frac{L}{2}\sin 50^\circ + \frac{L}{6}\sin 50^\circ = \frac{2}{3}L\sin 50^\circ$$

Now, we have

$$\sin 50^{\circ} = \frac{\overline{h}_{cp}}{y}$$
$$y = \frac{\frac{2}{3}L\sin 50^{\circ}}{\sin 50^{\circ}} = \frac{2}{3}L$$

 \Rightarrow

Thus the perpendicular distance of the line of action of the hydrostatic force F from the hinge is given by

Lever Arm =
$$L - \frac{2}{3}L - 2 = \frac{L}{3} - 2$$

Taking the moment of all the forces about the hinge, we get

$$F\left(\frac{L}{3}-2\right) = 0$$

$$\Rightarrow \quad \frac{WL^2}{2}\sin 50^\circ \left(\frac{L}{3}-2\right) = 0$$

$$\Rightarrow \qquad \qquad L = 6 \text{ m}$$

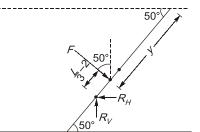
$$\therefore \qquad \qquad D = L \sin 50^\circ = 6 \sin 50^\circ = 4.6 \text{ m}$$

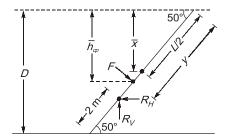
Now for equilibrium,

$$R_{H} = F \sin 50^{\circ} = \frac{WL^2}{2} \sin 50^{\circ} \times \sin 50^{\circ} = \frac{9810 \times (6)^2}{2} \times \sin^2 50^{\circ} = 103.62 \text{ kN}$$

$$R_V = F\cos 50^\circ = \frac{wL^2}{2}\sin 50^\circ \times \cos 50^\circ = \frac{9810 \times (6)^2}{2} \times \sin 50^\circ \times \cos 50^\circ = 86.95 \text{ kN}$$

Resultant Reaction, $R = \sqrt{R_H^2 + R_V^2} = \sqrt{(103.62)^2 + (86.95)^2} = 135.27 \text{ kN}$





2.2 Determine the total pressure on a plane rectangular plate 1 m wide and 3 m deep when its upper edge is horizontal and coincides with water surface and plate is held perpendicular to water surface. [2 marks : 2010]

Solution:

Let the width and depth of the rectangular plate be *b* and *d* respectively. Total pressure on the rectangular plate will be given as $P = \gamma A \overline{x}$ where γ is the unit weight of water, *A* is the area of rectangular plane surface and \overline{x} is the distance of centre of gravity from water surface. $\therefore \qquad P = \gamma \times b \times d \times \overline{x}$ $= 9810 \times 1 \times 3 \times \frac{3}{2}$ = 44145 N = 44.145 kN

Show that the hydraulic pressure remains invariant in a horizontal plane parallel to free surface. [4 marks : 2010]

Solution:

2.3

Consider an element of area dA, is y height below the free surface level, in a fluid of density ρ , hence for equilibrium $pdA + Weight of liquid in a volume of <math>dA \cdot dy = (p + dp)dA$ $pdA + \rho d (dAdy) = (p + dp)dA$ $pg \cdot dAdy = dp \cdot dA$ $\frac{dp}{dy} = \rho g$ $p = \rho gy + \text{constant}$ $p \propto y$ Hydrostatic pressure \propto Depth

Hence, hydrostatic pressure varies only in vertical direction. Hence at a particular depth below the free surface hydrostatic pressure will remain same in a horizontal plane.

2.4 A 45° sector gate is located on the crest of spillway. The water is upto the mid-point of the gate when closed. The width of the gate is 10 m. The radius of the sector gate is 2 m. Determine the hydrostatic force on the gate. Mass density 1000 kg/m³, g = 9.79 ms⁻².

[10 marks : 2011]

Solution:

Given: Radius of the sector gate = R = 2 m Width of the gate = I = 10 m

(idth of the gate
$$= L = 10$$
 m

Height of water, h above the bottom tip of the gate

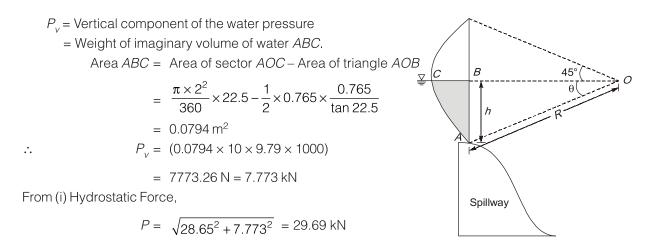
 $\Rightarrow \qquad \sin\theta = \frac{h}{R}$ $\Rightarrow \qquad h = R \sin\theta = 2 \sin 22.5 = 0.765 m$ Hydrostatic force, $P = \sqrt{P_{H}^{2} + P_{V}^{2}}$...(i) $P_{H} = \gamma_{w} A \overline{x}$

Here A is area of vertical projection of the gate and \overline{x} is the C.G. of the vertical projection from top.

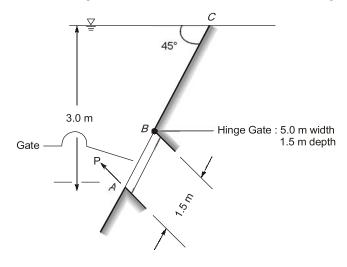
$$P_{H} = \gamma_{w} \cdot (h \times L) \times \frac{h}{2} = (9.79 \times 1000)(0.765 \times 10) \times \frac{0.765}{2}$$

= 28646.76 N = 28.65 kN





2.5 A rectangular gate of width 5 m and depth 1.5 m is installed to control the discharge as shown in figure below. The end 'B' is hinged. Determine the force normal to the gate applied at 'A' to open it.



[6 marks : 2012]

Solution:

Given: $A = \text{Area of gate} = 1.5 \times 5 = 7.5 \text{ m}^2$ Depth of C.G. of gate from free surface of water = \overline{h} = DG = AC - AE $= 3 - AG \sin 45^{\circ}$ $= 3 - 0.75 \times \frac{1}{\sqrt{2}}$ = 2.4697 mThe total pressure forms (O parting on the gate

The total pressure force (F) acting on the gate,

 $F = \rho g A \overline{h} = 1000 \times 9.81 \times 7.5 \times 2.4697 = 181708.18 \text{ N} = 181.71 \text{ kN}$ This force is acting at point *H* where depth of *H* from free surface is given by

$$h^* = \frac{I_G \sin^2 \theta}{A\overline{h}} + \overline{h}$$

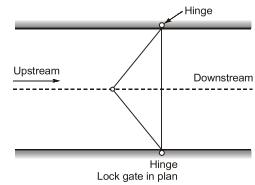
$$I_G = M.O.I \text{ of gate} = \frac{bd^3}{12} = \frac{5 \times 1.5^3}{12} = 1.40625 \text{ m}^4$$

where,

÷	Depth of centre of pressure	7* =	$\frac{1.40625 \times \sin^2 45^\circ}{7.5 \times 2.4697} + 2.4697$
		=	0.03796 + 2.4697 = 2.508 m
As	from figure sin 45	5° =	$\frac{h^*}{OH}$
÷	Distance, O	H =	$\frac{h^*}{\sin 45^\circ} = \frac{2.508}{\frac{1}{\sqrt{2}}} = 3.547 \mathrm{m}$
Dis	tance, A	0 =	$\frac{3}{\sin 45^\circ} = 4.243 \text{m}$
	Distance, A	Н =	<i>AO – OH = </i> 4.243 – 3.547 = 0.696 m
.:.	Distance B	Н =	<i>AB – AH</i> = 1.5 – 0.696 = 0.804 m
Taking the moments about the hinge <i>B</i>			
	$P \times A$	В =	$F \times (BH)$
<i>.</i> :.	$P \times 1$	5 =	181708.18×0.804
\Rightarrow		P =	<u>181708.18 ×0.804</u> = 97395.585 N = 97.396 kN
The gates of lock are 5 cm wide by 6 m and when			

2.6 The gates of lock are 5 cm wide by 6 m and when closed, at an angle of 120°. Each gate is held on by two hinges placed at the top and bottom of the gate. If the water levels are 6 m and 4.5 m on the upstream and downstream sides respectively, determine the magnitude of the forces on the hinges due to the water pressure.



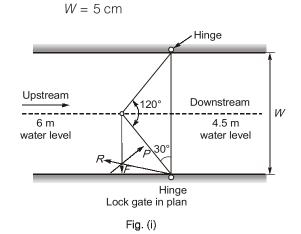


Solution:

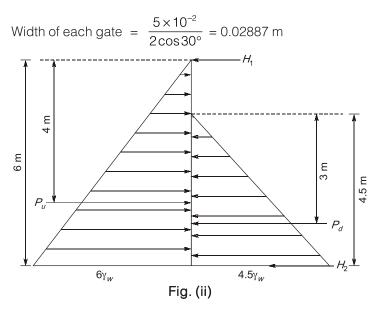
Width of the gates of lock = 5 cm

Although 5 cm width is practically not possible, it may be due to printing error in exam. Assuming data given is correct.

.: Width,







Total pressure on the upstream face of the gate is

$$P_u = \rho g \bar{h} A = 1000 \times 9.81 \times \frac{6}{2} \times [6 \times 0.02887]$$

The depth of the centre of pressure on the upstream face is given by

$$\overline{h}_{U} = \overline{h} + \frac{I_{CG}}{A\overline{h}} = 3 + \frac{\frac{1}{12} \times 0.02887 \times 6^{3}}{(0.02887 \times 6) \times 3} = 4 \text{ m}$$

Total pressure on the downstream face of the gate is

$$P_d = \rho g \overline{h} A = 1000 \times 9.81 \times \frac{4.5}{2} \times (0.02887 \times 4.5)$$
$$= 2867.5488 \text{ N} = 2.86755 \text{ kN}$$

Depth of centre of pressure on downstream face is

$$\overline{h}_d = \overline{h} + \frac{I_{CG}}{A\overline{h}} = 2.25 + \frac{\frac{1}{12} \times 0.02887 \times 4.5^3}{(0.02887 \times 4.5) \times 2.25} = 3 \text{ m}$$

Resultant water pressure on each gate

$$P = P_u - P_d = 5.0978 - 2.8675 = 2.2303 \text{ kN}$$

If x is the height of the point of application of the resultant water pressure on the gate, then

$$P \times x = P_u \times (6 - \overline{h}_u) - P_d \times (4.5 - \overline{h}_d)$$

$$\therefore \qquad 2.2303 \, x = 5.0978 \times (6 - 4) - 2.8675 \, (4.5 - 3)$$

$$x = 2.643 \, \text{m}$$

Consider Free Body Diagram from fig. (i), we get

 $2H_1$

6 m

F = R

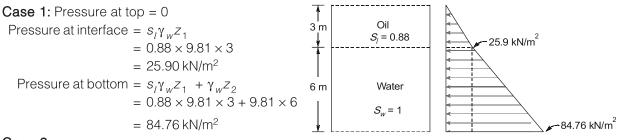


[8 marks : 2015]

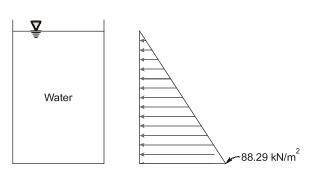
 $F\sin 30 + R\sin 30 = P$ Also, $R = \frac{P}{2\sin 30} = P = 2.2303 \text{ kN}$ Now, from fig. (iii) $R = 2H_1 + 2H_2$ $\Sigma F_{x} = 0;$ $R \times x = 2H_1 \times 6$ $\Sigma M_{H_2} = 0;$ Force on one top hinge, $H_1 = \frac{2.2303 \times 2.643}{6} = 0.4912 \text{ kN}$ *:*.. $2H_2 = R - 2H_1 = 2.2303 - 0.4912 = 1.7391 \text{ kN}$ *.*.. Force on on one bottom hinge, $H_2 = 0.6239 \text{ kN}$

2.7 A 9 m deep tank contains 6 m of water and 3 m of oil of relative density 0.88. Determine the pressure at the bottom of the tank. What is the pressure at the bottom of the tank if the entire tank is filled with water? What is the water thrust in this case? Draw the pressure distribution diagram in both the cases.

Solution:



Case 2:



Pressure at top = 0Pressure at bottom = $\gamma_w H = 9 \times 9.81 = 88.29 \text{ kN/m}^2$ Water thrust = $\frac{1}{2}(\gamma_w H) \times H = \frac{1}{2} \times 88.29 \times 9 = 397.305$ kN per meter width of wall

3. Buoyancy & Floatation

A metallic cube 30 cm side and weighing 450 N is lowered into a tank containing a two fluid layer 3.1 of water and mercury. Top edge of the cube is at water surface. Determine the position of block at water-mercury interface when it has reached equilibrium.

[10 marks : 2009]